Developing a Public Transit Scheduling Tool for Metro Manila Bus Operators

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Abstract: Philippine public land transport services are regulated by authorities through granting of franchises and setting of routes and fares. The operating structure enables a competitive environment among various operators with a wide range of operating schemes. Metro Manila bus operators would normally run their entire fleet since they perceive that this would generate the highest possible revenue. However, operating the entire fleet usually results to an unscheduled service. The lack of theoretical knowledge on bus service scheduling hinders local transport service providers in improving their service. Hence, this paper proposes a public transport scheduling tool for bus operators as a solution to these present issues. The tool could be run on spreadsheet software such as Microsoft Excel. It would enable users to input on-board passenger counts, to analyze and graph travel characteristics of a transit line, and to generate an efficient operating schedule. The scheduling tool and the theoretical background considered in its construction are discussed in this paper. The tool was tested using actual sample data from buses operating along the busiest corridor in Metro Manila - Epifanio Delos Santos Avenue (EDSA). Data analysis shows that the routes evaluated have: (1) low utilization ranging from 56-66% of the service capacity; (2) an average passenger trip length that accounts to about 24% of the trip length; (3) travel delays are about 32% of the total travel time. With such results, it is therefore beneficial to adjust the service capacity of the selected routes. Finally, the limitations of this scheduling tool were examined and corresponding recommendations were made to further improve it.

Key words: transit scheduling, computer-aided scheduling, public transport

1. INTRODUCTION

The role of public transportation is crucial to the development of any rapidly growing metropolis. In the case of the Philippine capital region, the economic and demographic growth of Metro Manila challenges and puts pressure to the existing public transport infrastructure and system. In order to maintain the growth and development of the economy, PT services should adapt to the growing demand for passenger travel within the metropolis. This paper discusses the development of a public transit scheduling tool that would provide transport operators a better understanding of their current transport service operations and provide an operating schedule to improve their level of service to transit users.

Bus transport service is regulated through a franchising system by the Land Transportation Franchising and Regulatory Board (LTFRB). The LTFRB controls the bus operators by granting Certificates of Public Conveyance (also known as franchises) and transit fares by setting fare matrices on regular bus services. Under the current system, transit service providers have freereign with the implementation of their operating schemes. Table 1 show that around 42% (5,343 of the 12,595) the buses in operation service the Metro Manila area. It also shows that buses operating EDSA have the greatest number of operating vehicles in the region. Among the routes in Metro Manila, the Alabang-SM Fairview via Lagro Commonwealth and the Baclaran-Novaliches via EDSA Mindanao Avenue were considered as the busiest inter-city routes. The franchising system, high number of operators and the highly perceived passenger demand for transport service have led to a competitive environment between transport operators and the practice of various illegal acts such as the operation of illegal or colorum buses or the proliferation of *"kabit system"* (practice of illegally using a different company's bus franchise to another company). Although the number of operating vehicles is high in the area, it neither translates to a highly utilized transport system nor good quality of service to transit users. It is known that inter-city bus operators do not practice scheduling of operations. The lack of information to commuters may lead to low satisfaction of transport service because of arbitrary arrival times at terminals or bus stops.

Route	Number of Operators	Number of Buses		
Manila EDSA Route	266	3,711		
Manila Non-EDSA Route	127	1,632		
Manila Provincial North Bound	371	3,684		
Manila Provincial South Bound	357	3,568		
TOTAL	1,122	12,595		

Source: LTFRB

The planning process of public transport operation includes four sequential activities: (1) network route design, (2) timetable development, (3) vehicle scheduling, and (4) crew scheduling (Ceder, 2007). It is advised to conduct the four activities in sequential order to maximize the productivity and efficiency of the bus operation. Considering the complexities of each activity, each process can be individually accomplished with each output being fed to its successor. Despite the benefits of public transport planning, local bus operators rarely conduct these processes due to the lack of expertise in the field and due to the costs that are attributed to it. Hence, operations are based on passenger demand that is only based on perception and experience.

In order to address the existing gap between methodologies in public transit scheduling and transport operators, a basic spreadsheet tool was developed. This tool would allow local transit providers record and analyze passenger data, and schedule departures of vehicles from a terminal or depot. Aside from the fact that almost all computers have spreadsheet programs such as Excel, spreadsheet programs have the ability to hold and analyze vast amounts of data while making it simple and user-friendly. The researchers believe that these tools would allow managers have a better understanding of the performance of their transit operations. They would also be adept in making informed decisions with regards to managing their bus fleet. In the end, commuters would benefit from this tool as it aims to make transport service more reliable in the form of consistent and scheduled departures and arrivals. This tool is tested in existing routes using actual passenger data and is shown in the succeeding sections.

2. LITERATURE REVIEW

This paper focuses on the development of a spreadsheet tool that enables transit managers record passenger data, analyze travel characteristics of transit service along the route, and schedule operations based on recorded passenger data. The researchers pursue the idea that managers need to have a better understanding of their fleet operations in order to improve the quality of bus services. This section would note the various studies related in transit scheduling and timetabling.

Scheduling of operations normally include the process of frequency setting and headway determination. For purposes of consistency, frequencies are set on specific time periods. Time periods are in accordance to the hour of the day and the day of the week (Guihaire & Hao, 2008) as demand may vary within the day and week. Four approaches were made by Furth and Wilson (1982) in determining headways of transit routes. The determined headways were policy headways, headways from maximum passenger load and vehicle capacity, headways wherein the ratio of revenues and expenses will not exceed a predetermined value, and headways designed to attain a desired passenger- or vehicle-miles. A heuristic method that included setting frequencies to a minimum in order to satisfy passenger demand and then uniformly increasing the

frequencies on different lines such that all vehicles would be used were proposed by Han and Wilson (1982). Four methods of frequency setting were suggested by Ceder (1984) depending on how data were gathered. Frequencies were determined by dividing the design load to the desired occupancy of the vehicle. The design loads can be the maximum daily load, the maximum hourly load, the average passenger load from the load profile diagram, or the passenger load at a certain percentage along the route. Finally, Vuchic (2007) proposed the use of peak hour coefficients in determining the hourly passenger volume used in frequencies setting. This coefficient takes into account the variability of the passenger volume within each time period.

In the local setting, a variety of studies that focus on scheduling of transit services were conducted. The studies of Kang, et al., (2011) and Dumalus, et al., (2012) adopted the methods of proposed by Ceder (1984) and Vuchic (2007) in the scheduling of jeepney services in Metro Manila and Iloilo City, respectively. Both researches used scheduling of transport service as a means of reducing the number of operating vehicles as it contributes to the congestion of roadways in their respective areas. Scheduling of services were also used to integrate transit operations and reduce passenger waiting times and transit dwell times at an intermodal terminal (Abad & Fillone, 2013).

All of the cited researches made use of a programming language or a spreadsheet software in their validation of results and production of schedules. The results, however, cannot reach local transport providers due to the latter's inability to interpret the actual results of the respective studies. The developed spreadsheet tool would address this gap by letting operators have actual control of producing their own schedule from their own data.

3. METHODOLOGY AND DEVELOPMENT OF THE SPREADSHEET TOOL

The program was developed from a spreadsheet program – Microsoft Excel. Aside from the fact that it is the most widely used spreadsheet software, Excel allows user to add programmable functions by running macros through an add-in called Visual Basic for Applications. The program was patterned after the three components of the scheduling process determined by Vuchic (2007). These components and its corresponding steps on the scheduling tool are shown in Figure 1.



Figure 1. Components of the Scheduling Process and Corresponding Steps in the Scheduling Tool

3.1 Data Input and Analysis

The data-gathering process is the most important component in the tool. It begins with a conduct of a ride check or on-board survey wherein the surveyor would board the vehicle, count the number of passengers boarding or alighting, and record the time the vehicle stopped or moved from certain locations. The data can be encoded to the tool by: (1) selecting or adding the route; (2) encoding the time and passenger movement for each predetermined stops. Step 1 lets user choose from a list of existing routes wherein their data will be recorded. Schedulers may also add specific routes with each checkpoint and its respective distances from their starting point or terminal. Step 2 allows the submission of encoded data wherein several transit line characteristics can be calculated. It is during data input that individual line characteristics are computed such as travel and running times and velocities, delays, and cumulative passenger boarding and alighting. Figure 2 shows the user interface in the actual steps involved.

The spreadsheet tool provides both numerical and graphical results on the travel characteristics for the given route. Each characteristic can be evaluated individually or wholly. The travel characteristics were based from the formulations of Vuchic (2007).



Figure 2. Data Input Process for the Spreadsheet Tool (a) Route Selection, (b) Route Addition, and (c) Actual Data Input

Average passenger trip lengths are obtained by dividing the total passenger-km (pax-km) to the total number of passengers along the line. Average passenger volume is the ratio of the total pax-km to the total line length. In equation form, these are as follows:

$$l_{av} = \frac{\sum_{i=1}^{n} p_i \cdot l_i}{p_t}$$
(1)

$$p_{av} = \frac{\sum_{i=1}^{n} p_i \cdot l_i}{L}$$
(2)

where l_{av}: average trip length (km) p_{av}: average passenger volume (pax) p_i: total passengers aboard the vehicle (pax) p_i: number of passengers for section *i* (pax) l_i: segment distance (km) L: transit line length (km)

Various coefficients are also calculated in order to describe the operations of the transport fleet. The coefficient of flow variations describes the changes in passenger volume peaks along the transit line. The lowest value for this coefficient is one (1). This is found on lines with constant passenger load on the duration of its whole transit operation. High values of this coefficient express low average load factors. This indicates that a desirable adjustment is needed to the offered service supply to existing passenger demand. Mathematically, the coefficient of flow variations is expressed as the ratio of the maximum volume to the average passenger volume shown as:

$$\eta_f = \frac{P_{\max}}{p_{av}} = \frac{L \cdot P_{\max}}{\sum_{i=1}^n p_i \cdot l_i}$$
(3)

where: η_f : coefficient of flow variations

Coefficient of passenger exchange describes the portion at which passenger volumes are exchanged along the transit line. It is the ratio of the total passengers who embarked the bus along the line but did not replace alighting passengers. Mathematically, it is calculated as:

$$\eta_{x} = \frac{P_{t}}{P_{t} - \sum_{i=1}^{n} |b_{i} - a_{i}|}$$
(4)

where: η_x : coefficient of passenger exchange

 b_i , a_i : number of passengers who boarded / alighted at segment *i* (pax)

The lowest value of 1 is attained when there is no passenger exchange along the line. The greatest value of this coefficient is realized when all passengers are exchanged at each stop along the route (L/l_{av}) .

Coefficient of work utilization shows the ratio of the utilized work to the offered transport work. The value simply represents how much of the offered capacity is actually utilized along the line. The load factor for each segment varies along the line and reaches its maximum at the maximum load section (MLS) where P_{max} is found. The coefficient is expressed as:

$$\overline{\alpha} = \frac{w_p}{w_o} = \frac{\sum_i p_i \cdot s_i}{C \cdot L}$$
(5)

where: $\overline{\alpha}$: coefficient of work utilization w_p: utilized work (pax-km) w_o: offered work (pax-km) C: vehicle capacity (pax)



Figure 3. Sample result showing travel characteristics for Coastal-Letre route and section analysis from Taft Rotonda to Estrella Stop

3.2. Scheduling Process and Output

The scheduling process is divided into three crucial steps: (1) frequency and headway determination, (2) timetable construction, and (3) vehicle scheduling. Headways are calculated using Equation 6. Load factor for Equation 6 can have a value up to 1.2 to account for standing passengers which is estimated at 20% of the total seating capacity. The actual value resulting from Equation 6 is compared to existing policy headways (if available). The minimum value will be adopted and converted to the nearest clock headway (6, 7.5, 10, 12, 15, 20, 30, and 60). The rounding down to the nearest clock headway is done to make the schedule easier to remember. Frequencies of departures for each time periods are then calculated after determining the design headway. The tool evaluates the new load factor under the proposed condition using Equation 8. The evaluation is done to let transit operators assess if the proposed schedule would yield higher utilization of supply. Timetables are automatically generated by the program depending on the parameters (capacity, load factor, terminal time). In order to effectively schedule each operating vehicle (trip-blocking), the tool would calculate the number of operating vehicles for operation using Equation 9. The formulations for each process are as follows:

$$h = \frac{60 \cdot \alpha \cdot n \cdot C_{\nu}}{P_d} \tag{6}$$

$$f = \frac{60}{h} \tag{7}$$

$$\alpha = \frac{P_d \cdot h}{60 \cdot n \cdot C_v} \tag{8}$$

$$N_{TU} = \left[\frac{T}{h}\right]^{+} = \left[\frac{f \cdot T}{60}\right]^{+}$$
(9)

where: h: headway (minutes)

 α : load factor, user-dependent (for equation 6 only)

n: number of transit units, n = 1 for buses

C_v: vehicle capacity (passengers)

P_d: passenger design volume (passengers)

f: frequencies of departures (vehicles/hour)

T: cycle time or two-way operating time including time spent on terminals (minutes)

4. DATA ANALYSIS AND RESULTS

The performance of the program was assessed by running sample data on various routes that operate along EDSA. As part of the analysis of this paper, transit service operations were evaluated using the program. Table 2 shows the summary results for the sample data.

Table 2. Travel characteristics for selected routes							
Route (Sample Size)	Line length, km	l _{av} , km	P _{av} , pax	η_{f}	η_x	α	
Fairview - Coastal via Commonwealth (12)	35.702	10.2	403	1.449	2.414	0.56	
Coastal - Fairview via Commonwealth (14)	33.74	8.496	436	1.684	2.358	0.519	
Alabang – Fairview (10)	43.342	10.765	396	1.76	2.287	0.66	
Fairview – Alabang (9)	43.55	11.95	286	1.574	2.315	0.831	
Letre – Coastal (4)	31.74	6.276	150	1.875	2.698	0.625	
Coastal – Letre (4)	27.69	7.164	153	1.308	2.955	0.637	
Letre - Coastal via Ayala (6)	33.345	5.84	193	1.774	3.219	0.537	
Coastal - Letre via Ayala (6)	29.91	6.435	227	1.815	2.561	0.631	
Coastal - Fairview via Mindanao (6)	31.08	8.089	214	1.725	2.227	0.596	
Fairview - Coastal via Mindanao Ave (6)	32.42	7.687	219	1.926	2.19	0.609	

Table 2. Travel characteristics for selected routes

Since the chosen sample routes all pass through EDSA, the respective line lengths are all greater than 25 kilometers. However, passenger trip lengths only average at around 18 - 29% of the total line length. Analysis of passenger load profile diagrams show that peak passenger loads occur at certain segments along the line. The location of peak passenger loads may occur at different segments along the line as shown in Figure 4. However, the program does not consider when the data was taken and may not take into account the variations in passenger demand within the day.



Figure 4. Passenger load profiles for selected routes

Figure 4 illustrates that some routes have greater passenger loads at the beginning of the routes while others at further sections of the routes. Graphical representations of passenger loads can be useful for transit operators to adjust their operations based on existing passenger demand. Transit managers could short-line their operations to minimize their costs by running shorter lengths but maximizing their revenue when operating on segments that have the greatest passenger demand.

Various coefficients that characterize current transport operations suggest that adjustment on service supply is desirable. Work utilization coefficients for all the sample routes show that, on average, about 56% - 66% (max. 83%) of the seating capacity (average capacity: 58) is utilized. Graphical representations of passenger loads corroborate with these values as most sections along the route are below the average passenger load. Coefficients of passenger flow (η_f) for all routes are all greater than one (1). The values suggest that passenger loads are not constant along the line and that service supply is greater than passenger demand. High passenger exchange for all routes was observed as shown by the coefficients of passenger exchange (η_x). Passenger movement can be illustrated by cumulative boarding and alighting profiles as shown in Figure 5. It can be seen in the figure that for all sections, passenger movement (whether boarding or alighting) was observed. High values illustrate that the cumulative alighting profile does not intersect the cumulative boarding profile. The calculations also confirm the assumption that the boarding and alighting profile only close at the last stop of the route.



Figure 5. Boarding and Alighting Profiles for Select Routes

Performance of operations can also be assessed by analyzing the time and speed it took for the vehicle to operate along the line. The average route running and travel times and velocities are presented in Table 3.

0	Lino	Running	Running	Traval	Traval	Total	
Route	length,	time,	velocity,	time,	velocity,	Delay,	
	km	mins	km/hr	mins	km/hr	mins	
Fairview - Coastal via	95 709	85.63	25.02	125.4	17.08	39.77	
Commonwealth	35./02						
Coastal - Fairview via	00 74	81.38	24.88	117.9	17.17	36.52	
Commonwealth	33./4						
Alabang - Fairview	43.342	82.34	31.583	122.107	21.297	39.767	
Fairview - Alabang	43.55	94.54	27.64	137.2	19.05	42.66	
Letre - Coastal	31.74	108.8	17.5	163.1	11.68	54.3	
Coastal - Letre	27.69	98.125	16.937	153.45	10.83	55.325	
Letre - Coastal via Ayala	33.345	93.53	21.39	143.9	13.9	50.37	
Coastal - Letre via Ayala	29.91	99.82	17.98	162	11.08	62.18	
Coastal - Fairview via	01.09	76.89	24.25	107.7	17.31	30.81	
Mindanao	31.00						
Fairview - Coastal via	00.40	87.61	22.2	117.7	16.53	30.09	
Mindanao Ave	32.42						

Table 3. Running and Travel Times and Velocities for Select Routes

The values in Table 3 show that running times for the vehicles exceed one hour for one way operation. The excessive running time can be attributed to poor traffic conditions and the lengthy operating routes. The delays were accounted in the computed travel time. On the average, travel delays contribute to 32% of the travel time. Delays can be either a result of traffic flow, traffic controls, waiting at stops for passengers, or passenger boardings or alightings. The excessive running and travel times resulted to low running and travel velocities. Low velocities may lead to passengers being unsatisfied with bus transit performance and may consider shifting to alternate modes of transport such as private vehicles or rail transit (MRT3). The program allows transit providers to see the relationships between the times and velocities for the whole route or for selected segments along the route.

In Figure 6, the time and velocity graphs are shown for the route Coastal – Letre via Ayala for the section with the maximum passenger load occurring in one of the stops. The graphs show that the greatest delay occurred at the beginning of the route. This is true since the main terminal for passengers going to EDSA is located along these segments. The high travel times on these sections result to significantly low travel velocities. Eventually, velocities increase along the Baclaran – DFA Libertad section wherein there is only minimal delays. The maximum passenger load section occurred at Mayapis section. From the terminal to the maximum load section, the work utilization coefficient is 1.041. The value shows that all seats in this section are utilized and around 4% of the total passengers are standing.



(Coastal to Mayapis Section)

The spreadsheet tool allows the user to adjust the operating characteristics of their fleet in the scheduling of bus service operations. These characteristics include terminal time (time a vehicle is in the terminal before being dispatched for service), policy headway (headway that is being currently implemented, if any), utilization coefficient, and capacity of each vehicle (may vary if different bus manufacturers were used). Design passenger volume would depend on the data that was used in the program. Shown in Figure 7 is the interface for the scheduling of the route Coastal – Fairview via Mindanao Avenue. For this route, 6 buses per vehicle operating on 10-minute headways were suggested. Although the prescribed utilization coefficient for the route is 1.2, the anticipated coefficient of utilization for this kind of operation is 1.03. The difference could be a result of the variations in work utilization along certain sections in the route. Nevertheless, the operation ensures that almost all seats would be utilized in this type of operation. Scheduling results for the sample data are shown in Table 4.

Coastal - Fairview v. Mindanao	Ave	Transit Scheduling
Scheduling components for the tra	ansit line	
Passenger Volume		Operating Characteristics
I. Maximum Passenger Volume	370 pax/hr	IV. Minimum terminal time, t _t 5 mins
II. Average Passenger Volume	214 pax/hr	V. Policy headway, h _o 30 mins
III. One-way operating time, To	107.7 minutes	VI. Utilization coefficient, α 1.2 select value
		VII. Capacity of each vehicle 60 pax
Frequency, Headway, Fleet Size		Choose start of hourly time period: 7:00
I. Hourly Frequencies	6 veh/hr	III. Actual Load Factor 1.03
II. Actual Headway	0:10 min/veh	IV. Vehicle Fleet Size 11
Timetable		
First predetermined departu	re: 7:00	
Succeeding scheduled depart	ures:	
1 7:10 7	13	
2 7:20 8	14	
3 7:30 9	15	
4 7:40 10	16	
5 7:50 11	17	
6 8:00 12	18	J

Figure 7. User Interface for Transit Scheduling (Coastal - Fairview via Mindanao)

Table 4. Scheduling Results for Selected Routes							
Route	CurrentProposeRoutefrequency, αfrequencyvehvehveh		Proposed frequency, veh	Headway	Estimated α		
Fairview - Coastal via Commonwealth	12	0.56	10	6	0.97		
Coastal - Fairview via Commonwealth	14	0.519	10	6	1.2		
Alabang - Fairview	10	0.66	10	6	1.16		
Fairview - Alabang	9	0.831	8	7.5	0.94		
Letre - Coastal	4	0.625	3	20	1.11		
Coastal - Letre	4	0.637	4	15	1.2		
Letre - Coastal via Ayala	6	0.537	5	12	1.14		
Coastal - Letre via Ayala	6	0.631	6	10	1.14		
Coastal - Fairview via Mindanao	6	0.596	6	10	1.03		
Fairview - Coastal via Mindanao Ave	6	0.609	6	10	1.17		

Note: Schedules assume the following operating characteristics: terminal time: 5 minutes, policy headway: 30 minutes, utilization coefficient: 1.2, and seating capacity: 60

Tabulated above are the scheduling results for the selected EDSA routes. The scheduled service resulted to an equal or smaller number of frequencies. The adjustment on service frequencies is a result of the reduction on the offered capacity. Other routes have maintained their service frequencies but adjustments can be further made on the headways between vehicles. The resulting schedules also resulted to a high utilization of service (90 – 120%). The values show that the scheduled service increased the utilization coefficient by about 82%.

5. CONCLUSIONS AND RECOMMENDATIONS

Bus transit operations should be improved in view of the high passenger volume passing through major thoroughfares especially EDSA. The researchers developed a public transit scheduling tool based on Microsoft Excel in order to address the gap between existing literature on public transport scheduling and the tools that local transport providers currently use. With this, transport providers can analyze and manage their own data and schedule their operations based on their own operating constraints.

Sample results show that the program is very capable in handling extensive data input and analysis. The use of macros made repetitive tasks simpler and made analysis easier. Graphical and numerical results would let transit managers have an actual assessment of their current transport operations.

The sample results also show the condition of bus operations for selected bus routes that pass through EDSA. First, utilization of buses along the whole line is limited to 40%-60% of the total service supply being offered. Second, average trip lengths of passengers are around 30% of the total trip length. Third, maximum load sections are concentrated on certain segments of the total route. At such points, passenger loads are above average while the remainder has low passenger volumes, often, below average. Fourth, delays account to around 33% of the total travel time which makes travel slow and unsatisfactory for passengers. Despite travel delays being a result of a variety of factors, transit operators can adjust their operations to minimize travel delays. The data show that bus operations are underutilized as a result of poor operating conditions. The short trip lengths can be viewed negatively since bus fares are higher than its rail (MRT) counterparts. As a result, there is a need to adjust or to improve the operations of current bus service providers. Proposed adjustments on service capacities resulted to the decrease in frequencies of service. The reduction of service capacity and provision of scheduled service yielded to an anticipated increase of utilization by 82%.

The scheduling tool is still a work in progress and is being improved to add more features for operational analysis such as cost and revenue estimation and sustainability and co-benefit analysis. There is also a need to address certain issues on the data-input stage of the spreadsheet tool such as data input for skipped segments or sections on on-board surveys. The researchers are also addressing certain compatibility issues in order to make sure that the program would run across all Excel platforms. The researchers highly suggest the creation of stand-alone executable programs using other programming languages. Other methods of performing transit scheduling that can be programmed are highly recommended.

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